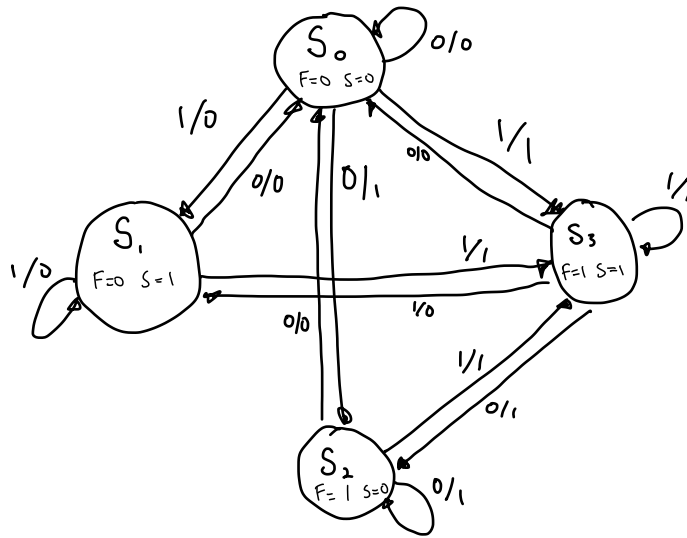


1 a) Draw the state diagram for a FSM to represent the given specifications.



1 b) Write an encoded state table (transition table) corresponding to the state diagram above.

Present State		Next State F+ S+			
F	S	DT = 00	DT = 01	DT = 10	DT = 11
0	0	$S_0 \xrightarrow{F+S+} 00$	$S_2 \xrightarrow{F+S+} 10$	$S_1 \xrightarrow{F+S+} 01$	$S_3 \xrightarrow{F+S+} 11$
0	1	$S_0 \rightarrow 00$	NA $\rightarrow$ /	$S_1 \xrightarrow{F+S+} 01$	$S_3 \xrightarrow{F+S+} 11$
1	0	$S_0 \rightarrow 00$	$S_2 \rightarrow 10$	NA $\rightarrow$ /	$S_3 \xrightarrow{F+S+} 11$
1	1	$S_0 \rightarrow 00$	$S_2 \rightarrow 10$	$S_1 \xrightarrow{F+S+} 01$	$S_3 \xrightarrow{F+S+} 11$

1 c) Fill in the Karnaugh maps for F+ and S+ and write minimal sum-of-products equations for F+, S+ (show your work).

FS\DT	00	01	11	10
00	0	1	1	0
01	0	X	1	0
11	0	1	1	0
10	0	1	1	X

F+

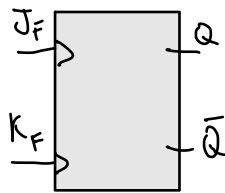
T

FS\DT	00	01	11	10
00	0	0	1	1
01	0	X	1	1
11	0	0	1	1
10	0	0	1	X

S+

D

1 d) Create the Karnaugh maps for J_F and K_F , J_S and K_S write minimal sum-of-products equations for each



FS\DT	00	01	11	10
00	0	1	1	0
01	0	X	1	0
11	X	X	X	X
10	X	X	X	X

J_F

FS\DT	00	01	11	10
00	X	X	X	X
01	X	X	X	X
11	1	0	0	1
10	1	0	0	X

K_F

J	K	Q	Q'	State
0	0	Q	Q'	no change
0	1	0	1	reset
1	0	1	0	Q=1
1	1	-	-	toggle

$$J_F = T$$

$$K_F = \overline{T}$$

FS\DT	00	01	11	10
00	0	0	1	1
01	X	X	X	X
11	X	X	X	X
10	0	0	1	X

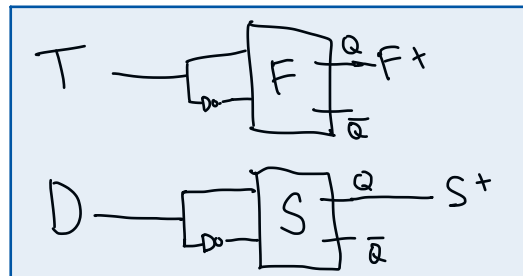
J_S

FS\DT	00	01	11	10
00	X	X	X	X
01	1	X	0	0
11	1	1	0	0
10	X	X	X	X

K_S

$$J_S = D$$

$$K_S = \overline{D}$$



2 a) Complete a state table corresponding to the state diagram.

present state	condition				next state
	A	B	C	D	
S_1	1	x	x	x	S_2
S_1	x	1	x	x	S_2
S_1	0	0	x	x	S_1
S_2	x	0	0	x	S_3
S_2	x	1	1	x	S_2
S_2	x	0	1	x	S_4

S_2	x	1	0	x	S_4
S_3	0	x	1	x	S_3
S_3	0	x	0	x	S_2
S_3	1	x	1	x	S_2
S_3	1	x	0	x	S_4
S_4	x	x	0	0	S_3
S_4	x	x	1	x	S_1
S_4	x	x	x	1	Z_1

2 b) Complete the encoded state table (transition table).

present state	condition				next state
XY	A	B	C	D	X^+Y^+
10	1	x	x	x	11
10	x	1	x	x	11
10	0	0	x	x	10
11	x	0	0	x	00
11	x	1	1	x	11
11	x	0	1	x	01
11	x	1	0	x	01
00	0	x	1	x	00
00	0	x	0	x	11
00	1	x	1	x	11
00	1	x	0	x	01
01	x	x	0	0	00
01	x	x	1	x	10
01	x	x	x	1	10

2 c) Fill in the Karnaugh maps for the next states X^+ , Y^+ .

AB\CD	00	01	11	10
00	1	1	0	0
01	1	1	0	0
11	0	0	1	1
10	0	0	1	1

XY=00

AB\CD	00	01	11	10
00	0	1	1	1
01	0	1	1	1
11	0	1	1	1
10	0	1	1	1

XY=01

Maps for X^+

$$D + C$$

AB\CD	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

XY=10

AB\CD	00	01	11	10
00	0	0	0	0
01	0	0	1	1
11	0	0	1	1
10	0	0	0	0

XY=11

$$\bar{A}\bar{C} + AC + D + C + BC$$

AB\CD	00	01	11	10
00	1	1	0	0
01	1	1	0	0
11	1	1	1	1
10	1	1	1	1

XY=00

AB\CD	00	01	11	10
00	0	0	0	0
01	0	0	0	0
11	0	0	0	0
10	0	0	0	0

XY=01

$$\bar{C} + A$$

Maps for Y^+

$$0$$

AB\CD	00	01	11	10
00	0	0	0	0
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

XY=10

AB\CD	00	01	11	10
00			1	1
01			1	1
11			1	1
10			1	1

XY=11

$$B + A$$

$$B + C$$

$$\bar{C} + A + B + C$$

2 d) Fill in the maps for each of D_X and D_Y .

AB\CD	00	01	11	10
00	1	1	0	0
01	1	1	0	0
11	0	0	1	1
10	0	0	1	1

XY=00

$\bar{Y}\bar{A}\bar{C}$

$\bar{Y}AC$

Map for D_X

AB\CD	00	01	11	10
00	0	1	1	1
01	0	1	1	1
11	0	1	1	1
10	0	1	1	1

XY=01

YBC $\bar{X}YD$ $\bar{X}YC$

AB\CD	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

XY=10

$X\bar{Y}$

AB\CD	00	01	11	10
00	0	0	0	0
01	0	0	1	1
11	0	0	1	1
10	0	0	0	0

XY=11

AB\CD	00	01	11	10
00	1	1	0	0
01	1	1	0	0
11	1	1	1	1
10	1	1	1	1

XY=00

$\bar{X}\bar{Y}\bar{C}$

AB\CD	00	01	11	10
00	0	0	0	0
01	0	0	0	0
11	0	0	0	0
10	0	0	0	0

XY=01

$\bar{X}Y$

AB\CD	00	01	11	10
00	0	0	0	0
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

XY=10

$\bar{Y}A$

Map for D_Y

AB\CD	00	01	11	10
00	0	0	1	1
01	1	1	1	1
11	1	1	1	1
10	0	0	1	1

XY=11

XB XYC

2 e) Determine the minimal sum-of-products equations for each of D_X and D_Y .

$$D_X = X\bar{Y} + YBC + \bar{X}Y\bar{A} + \bar{X}Y C + \bar{Y}\bar{A}\bar{C} + \bar{Y}AC$$

$$D_Y = \bar{X}\bar{Y}\bar{C} + \bar{Y}A + YB + XYC$$

2 f) Draw the circuit

